

GeoGebra Dynamic  
Worksheet: Ellipse 1  
Answer Sheet

Go to [www.doublecrosseducation.com/fetc.htm](http://www.doublecrosseducation.com/fetc.htm). Click on Ellipse 1.  
This shows the graph of the ellipse in the form:

$$\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1$$

You can manipulate the graph by changing the value(s) of  $h$ ,  $k$ ,  $a$ , and  $b$  which are called the **parameters** of the equation. In this worksheet we will examine how each of these parameters changes the graph of the ellipse.

- Start with  $h = 0$ ,  $k = 0$  and  $a = 2$ ,  $b = 3$ .
  1. Write the equation of this ellipse using the form above (NOT the form shown on the worksheet)  $\frac{x^2}{4} + \frac{y^2}{9} = 1$
  2. What is the orientation (horizontal or vertical) of the ellipse? *Vertical*
  3. Write the coordinates of:
    - i. the center  $(0,0)$
    - ii. the endpoints of the major axis  $(0,3)$   $(0, -3)$
    - iii. the endpoints of the minor axis  $(2, 0)$   $(-2,0)$
  
- Set  $h = 0$ ,  $k = 0$ ,  $a = 3$ ,  $b = 2$ .
  4. Write the equation for this ellipse.  $\frac{x^2}{9} + \frac{y^2}{4} = 1$
  5. What is the orientation (horizontal or vertical) of the ellipse? *Horizontal*
  6. Write the coordinates of:
    - i. the center  $(0,0)$
    - ii. the endpoints of the major axis  $(3,0)$   $(-3,0)$
    - iii. the endpoints of the minor axis  $(0, 2)$   $(0, -2)$

- Set  $h = 2, k = 0, a = 2, b = 3$ .

7. Write the equation for this ellipse.  $\frac{(x-2)^2}{4} + \frac{y^2}{9} = 1$

8. Write the coordinates of:

- the center  $(2,0)$
- the endpoints of the major axis  $(2,3) (2, -3)$
- the endpoints of the minor axis  $(0, 0) (0, 4)$

- Set  $h = -2, k = -1, a = 2, b = 5$ .

9. Write the equation for this ellipse.  $\frac{(x+2)^2}{4} + \frac{(y+1)^2}{25} = 1$

10. Write the coordinates of:

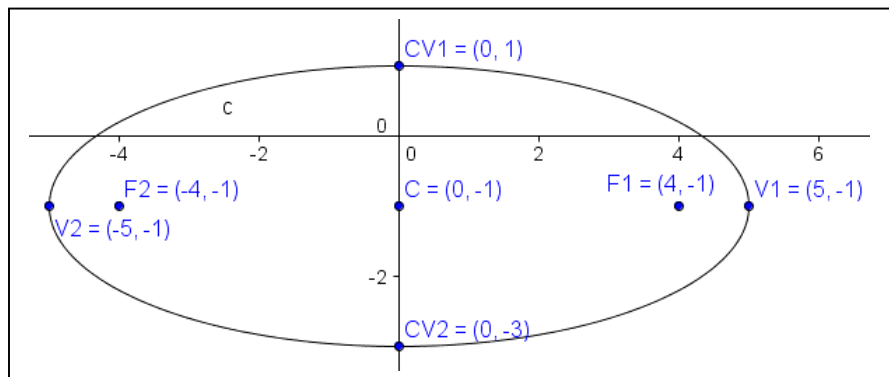
- the center  $(-2, -1)$
- the endpoints of the major and minor axis  
*Major:*  $(-2,4) (-2,-6)$   
*Minor:*  $(0,-2) (-4,-2)$

- Summarize how changing the value of  $h$  and  $k$ ,  $a$  and  $b$  in the equation affects the graph of the ellipse. Include any effects on the center, major and minor axes.

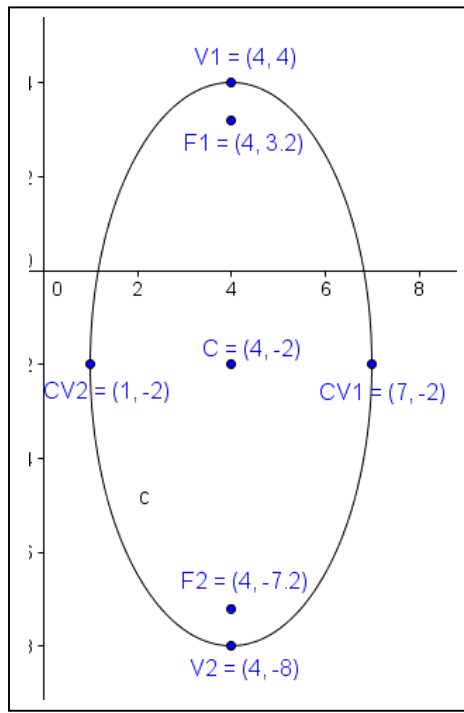
*The values  $h$  and  $k$  control the position of the center of the ellipse. The  $a$  and  $b$  values are the distance from the center to the vertices ( $a$ ) and co-vertices ( $b$ ). In an ellipse  $a > b$  and if  $a$  is in the denominator of the  $x^2$ , then the ellipse is horizontal. If  $a$  is in the  $y^2$  denominator, the ellipse is vertical.*

Use the Dynamic Worksheet to help you to sketch a graph of each of the ellipses below. Show the location of the center, endpoints of major and minor axes.

9.  $\frac{x^2}{25} + \frac{(y+1)^2}{4} = 1$

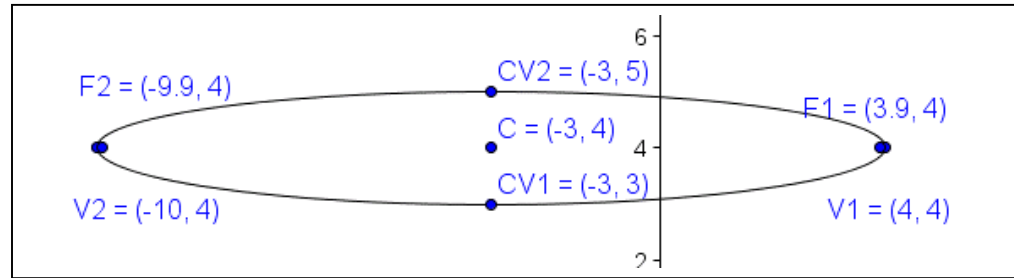


10.  $\frac{(x-4)^2}{9} + \frac{(y+2)^2}{36} = 1$



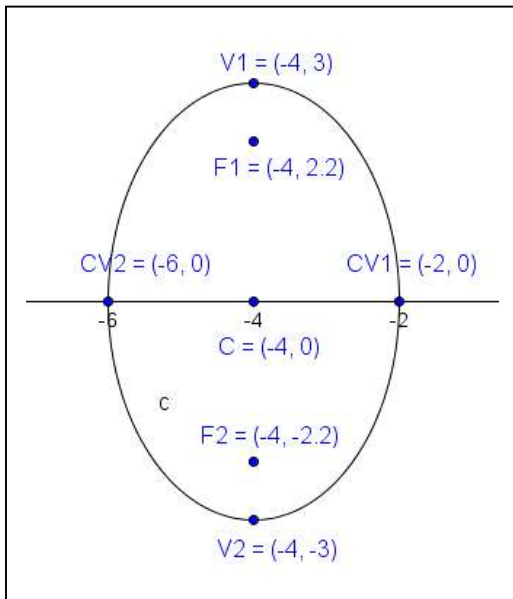
11.

$\frac{(x+3)^2}{49} + (y-4)^2 = 1$

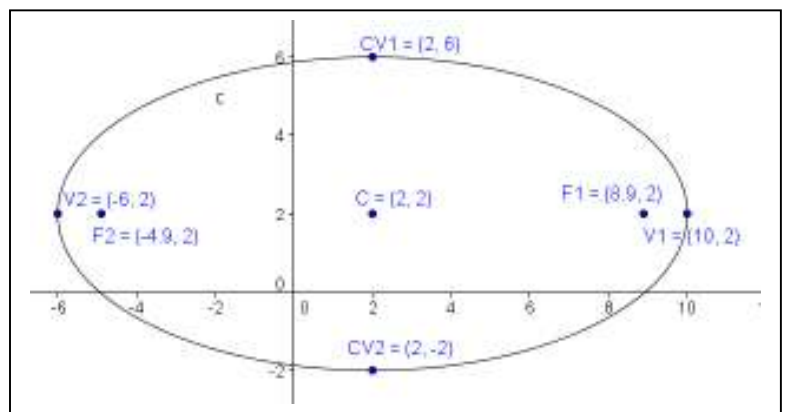


Graph each ellipse below without using the Dynamic Worksheet.

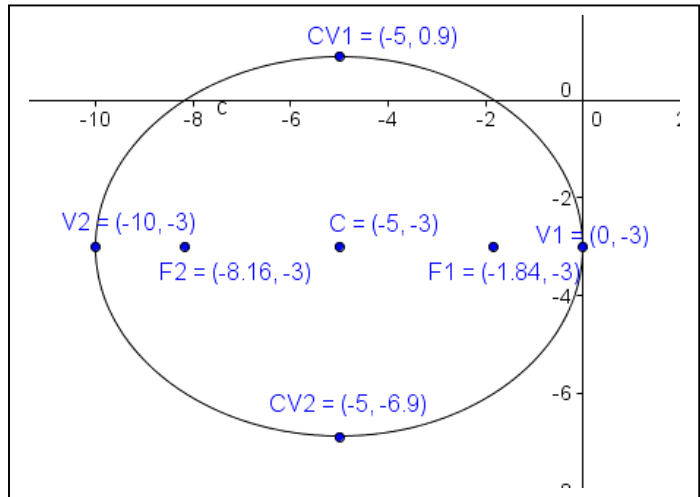
12.  $\frac{(x+4)^2}{4} + \frac{y^2}{9} = 1$



13.  $\frac{(x-2)^2}{64} + \frac{(y-2)^2}{16} = 1$



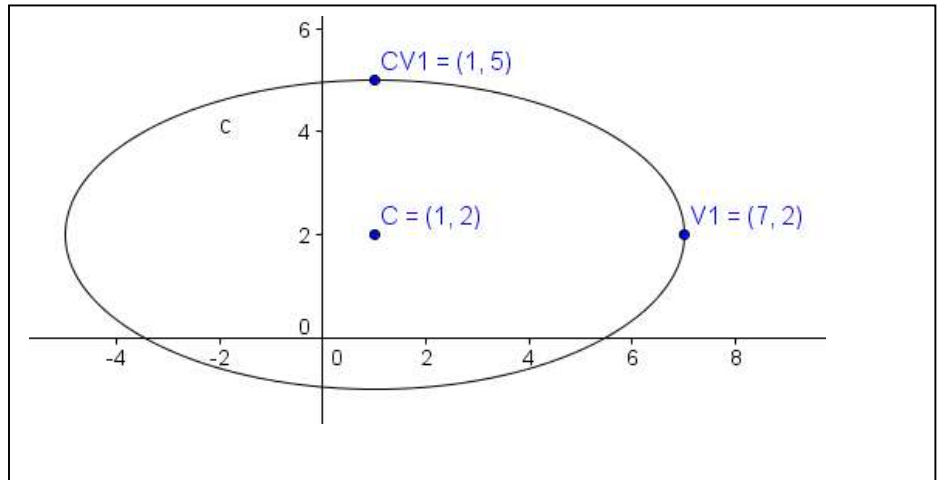
14.  $\frac{(x+5)^2}{25} + \frac{(y+3)^2}{15} = 1$



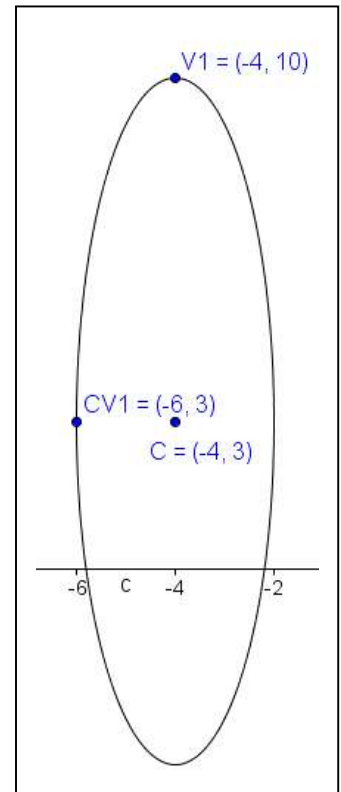
Write the equation for each ellipse shown below.

15.

$\frac{(x-1)^2}{36} + \frac{(y-2)^2}{9} = 1$



16.  $\frac{(x+4)^2}{4} + \frac{(y-3)^2}{49} = 1$



17.  $\frac{(x-1)^2}{36} + (y-3)^2 = 1$

